

225.

**Problem 20.57P (HRW)**

*Two containers are at the same temperature. The first contains gas with pressure  $p_1$ , molecular mass  $m_1$ , and root mean square speed  $v_{rms1}$ . The second contains gas with pressure  $2p_1$ , molecular mass  $m_2$ , and average speed . We have to find the mass ratio  $m_1/m_2$ .*

**Solution:**

At temperature T, the average speed  $\bar{v}$  is given by the relation



$$\bar{v} = \sqrt{\frac{8kT}{\pi m}},$$

where  $m$  is molecular mass. And the root-mean-square (rms) speed  $v_{rms}$  is given by

$$v_{rms} = \sqrt{\frac{3kT}{m}}.$$

We have been given that

$$\bar{v}_2 = 2v_{rms1}.$$

This implies that

$$\sqrt{\frac{8kT}{\pi m_2}} = \sqrt{\frac{3kT}{m_1}},$$

or

$$\frac{8kT}{\pi m_2} = \frac{4 \times 3kT}{m_1},$$

or

$$\frac{m_1}{m_2} = \frac{3\pi}{2} = 4.71$$

