

220.

Problem 24.5 (RHK)

At standard temperature and pressure (0°C and 1.0 atm) the mean free path in helium gas is 285 nm. We have to determine (a) the number of molecules per cubic meter and (b) the effective diameter of the helium atoms.

Solution:

(a)

The equation of state of an ideal gas in terms of the total number of molecules N at temperature T , pressure P and volume V is

$$P = \frac{N}{V} kT,$$

or

$$\begin{aligned} \rho_n = \frac{N}{V} &= \frac{P}{kT} = \frac{1.01 \times 10^5}{1.38 \times 10^{-23} \times 273.16} \text{ molecules. m}^{-3} \\ &= 2.68 \times 10^{25} \text{ molecules. m}^{-3}. \end{aligned}$$

(b)

The mean free path λ is determined by the number density of molecules ρ_n and the effective molecular diameter d by the relation

$$\lambda = \frac{1}{\sqrt{2}\pi d^2 \rho_n},$$

or

$$d = \left(\frac{1}{\sqrt{2}\pi\lambda\rho_n} \right)^{1/2}.$$

We are given that the mean free path in the helium gas at the standard temperature and pressure is

$$\lambda = 285 \times 10^{-9} \text{ m.}$$

Therefore,

$$d = \left(\frac{1}{\sqrt{2}\pi \times 285 \times 10^{-9} \times 2.68 \times 10^{25}} \right)^{1/2} \text{ m} = 1.71 \times 10^{-10} \text{ m}$$
$$= 0.171 \text{ nm.}$$