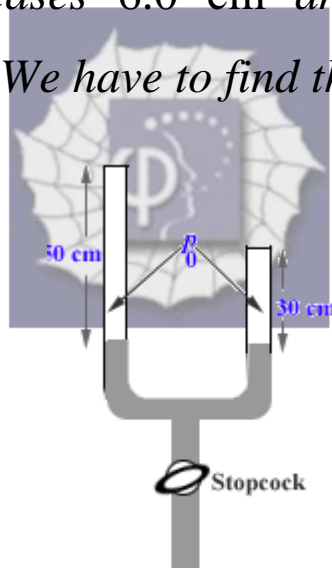


209.

Problem 23.16 (RHK)

A mercury-filled manometer with two unequal-length arms of the same cross-sectional area is sealed off with the same pressure p_0 in the two arms. With the temperature constant, an additional 10.0 cm^3 of mercury is admitted through the stopcock at the bottom. The level on the left increases 6.0 cm and that on the right increases 4.0 cm . We have to find the pressure p_0 .



Solution:

Let the cross-sectional area of the arms of the manometer be $a \text{ cm}^2$. The initial volume of the gas in the left-arm of the manometer will be

$$V_l = 50a \text{ cm}^3,$$

and the initial volume of the right-arm of the manometer will be

$$V_r = 30a \text{ cm}^3.$$

It is given that the pressure of gas in both arms of the manometer is p_0 .

When at constant initial temperature an additional 10.0 cm^3 of mercury is introduced in the manometer it is given that the level of mercury in the left-arm rises by 6.0 cm and that in the right-arm by 4.0 cm . The changed volume of the gas in the left-arm after mercury has been added will be

$$V_l' = 44a \text{ cm}^3,$$

and the changed volume of the gas in the right-arm will be

$$V_r' = 26a \text{ cm}^3.$$

Let the changed pressure in the left-arm be p_l' and that in the right-arm be p_r' . As the temperature has remained constant in the process, we have

$$44p_l' = 50p_0,$$

or

$$p_l' = \frac{50}{44} p_0.$$

Similarly, we have

$$26 p_r' = 30 p_0 ,$$

or

$$p_r' = \frac{30}{26} p_0 .$$

We now require that at the same level of mercury in both the arms of the manometer the pressure has to be equal.

This gives the condition

$$p_l' + \rho g \times 6 \times 10^{-2} = p_r' + \rho g \times 4 \times 10^{-2} ,$$

or

$$(p_r' - p_l') = \rho g \times 2 \times 10^{-2} ,$$

or

$$p_0 \left(\frac{30}{26} - \frac{50}{44} \right) = 13.6 \times 10^3 \times 9.8 \times 2 \times 10^{-2} \text{ Pa},$$

or

$$p_0 = 1.52 \times 10^5 \text{ Pa} = 1.5 \text{ atm}.$$