Problem 55.38 (RHK)

We have to calculate the Coulomb barrier height for two 7 Li nuclei, fired at each other with the same initial kinetic energy K.

Solution:

Using the empirical relation

$$R = R_0 (A)^{1/3}, R_0 = 1.2 \times 10^{-15} \text{ m},$$

we will determine the radius of ⁷Li nucleus.

$$R_{7_{\text{Li}}} = 1.2 \times (7)^{1/3} \text{ fm} = 2.295 \times 10^{-15} \text{ m}.$$

We assume that the two nuclei of 7 Li which are approaching each other with equal kinetic energy K are able to come to a stop when they are separated by $2R_{^{7}\text{Li}}$.

The height of their Coulomb barrier will be

$$U_{\text{coulomb}} = \frac{(3e)^2}{4\pi\varepsilon_0 \times (2R_{7_{\text{Li}}})}$$

$$= \frac{(8.99 \times 10^9) \times (3 \times 1.6 \times 10^{-19})^2}{2 \times 2.295 \times 10^{-15}} \text{ J}$$

$$= 45.126 \times 10^{-14} \text{ J}$$

$$= \frac{45.126 \times 10^{-14} \text{ J}}{1.6 \times 10^{-13}} \text{ MeV} = 2.82 \text{ MeV}.$$

The two ⁷Li nuclei will be able to overcome the Coulomb barrier height if they approach each other with

$$K = \frac{U_{\text{coulomb}}}{2} = 1.41 \text{ MeV}.$$

