

848.

**Problem 54.65 (RHK)**

*An 87-kg worker at a breeder reactor plant accidentally ingests 2.5 mg of  $^{239}\text{Pu}$  dust.  $^{239}\text{Pu}$  has a half-life of 24,100 y, decaying by alpha decay. The energy of the emitted  $\alpha$  particles is 5.2 MeV, with a quality factor of 13. We may assume that the plutonium resides in the worker's body for 12 h, and that 95% of the emitted  $\alpha$  particles are stopped within the body. We have to calculate (a) the number of plutonium atoms ingested; (b) the number that decay during the 12 h; (c) the energy absorbed by the body; (d) the resulting physical dose in rad; and (e) the equivalent biological dose in rem.*

**Solution:**

(a)

The number of  $^{239}\text{Pu}$  atoms in 2.5 mg of  $^{239}\text{Pu}$  dust will be

$$N = \frac{6.02 \times 10^{23} \times 2.5 \times 10^{-3} \text{ g}}{239 \text{ g}} = 6.29 \times 10^{18}.$$

(b)

The half-life of  $^{239}\text{Pu}$  is 24,100 y. Therefore, its disintegration constant will be

$$\lambda = \frac{\ln 2}{24,100 \times 3.156 \times 10^7 \text{ s}} = 9.11 \times 10^{-13} \text{ s}^{-1}.$$

The decay rate of  $6.29 \times 10^{18}$   $^{239}\text{Pu}$ -nuclides will be

$$\begin{aligned} R = N\lambda &= 6.29 \times 10^{18} \times 9.11 \times 10^{-13} \text{ s}^{-1} \\ &= 5.73 \times 10^6 \text{ disintegrations per second.} \end{aligned}$$

Therefore, of the  $6.29 \times 10^{18}$   $^{239}\text{Pu}$ -nuclides that would have decayed in 12 h will be

$$5.73 \times 10^6 \times 12 \times 3600 = 2.47 \times 10^{11}.$$

(c)

The energy of the emitted  $\alpha$  particles is 5.2 MeV, with a quality factor of 13 and that 95% of the emitted  $\alpha$  particles are stopped within the body. Therefore, the energy absorbed by the body will be

$$\begin{aligned} &= 2.47 \times 10^{11} \times 5.2 \times 1.6 \times 10^{-13} \times 0.95 \text{ J} \\ &= 195.6 \text{ mJ.} \end{aligned}$$

(d)

The strength of radiation is defined as 1 rad if  $10^{-5} \text{ J g}^{-1}$  of energy is absorbed by the body. Therefore, the resultant physical dose will be

$$\frac{195.6 \times 10^{-3} \text{ J}}{87 \times 10^3 \text{ g}} = 2.25 \times 10^{-6} \text{ J g}^{-1} = 0.225 \text{ rad.}$$

(e)

As the quality factor of alpha particle radiation is 13, the equivalent biological dose will be  $0.225 \times 13 \text{ rem} = 2.9 \text{ rem}$ .

