810.

Problem 53.38 (RHK)

A sample of pure germanium has one impurity atom to 1.3×10^9 atoms of germanium. We have to calculate the distance between impurity atoms.

Solution:

From the physical data of germanium we calculate the number of germanium atoms per cubic meter. The physical data for germanium are: molar mass of germanium, $M_{Ge} = 72.61$ g mol⁻¹, density of germanium, $\rho_{Ge} = 5.323$ g cm⁻³.

Therefore, the number of germanium atoms per cubic meter is given by

$$n_{_{\text{Ge}}} = \frac{N_A \rho_{_{\text{Ge}}}}{M_{_{\text{Ge}}}} = \frac{6.02 \times 10^{23} \text{ mol}^{-1} \times 5.323 \times 10^3 \text{ kg m}^{-3}}{72.61 \times 10^{-3} \text{ kg mol}^{-1}}$$
$$= 4.41 \times 10^{28} \text{ m}^{-3}.$$

It is given that a sample of pure germanium has one impurity atom to 1.3×10^9 atoms of germanium. Therefore, the number of impurity atoms per cubic meter in that sample of germanium will be

$$\frac{4.41 \times 10^{28}}{1.3 \times 10^{9}} = 3.39 \times 10^{19} .$$

Therefore, the average distance between impurity atoms will be

$$a = \left(\frac{1}{3.39 \times 10^{19}}\right)^{\frac{1}{3}} \text{ m} = 3.09 \times 10^{-7} \text{ m} = 309 \text{ nm}.$$

