Problem 51.8 (RHK)

We have to find the value of the quantum number for a hydrogen atom that has an orbital radius of 847 pm.

Solution:

The radii of the stationary states of hydrogen atom are given by the equation

$$r_n = n^2 a_0, \ n = 1, 2, 3...$$

Bohr radius
$$a_0 = \frac{4\pi\varepsilon_0 h^2}{me^2} = 52.92 \text{ pm}.$$

Therefore, the shell with orbital radius of 847 pm will correspond to principal quantum number n given by the equation

$$52.92 \times n^2 = 847$$

or

$$n^2 = \frac{847}{52.92} = 16.00,$$

and

$$n=4$$
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