

620.

**Problem 44.24 (RHK)**

*We have to show that the distance between a real object and its real image formed by a thin converging lens is always greater than or equal to four times the focal length of the lens.*

**Solution:**

As we are considering a real object and its real image formed by a thin converging lens, in the sign conventions that we are using the object distance  $o$ , and the image distance  $i$  will be real and positive numbers. The focal length  $f$  of a converging lens is also a real positive number. Let us call the distance between the object and its real image  $d$ . We have

$$d = o + i.$$

We consider the thin lens equation

$$\frac{1}{o} + \frac{1}{i} = \frac{1}{f},$$

or

$$\frac{1}{(d-i)} + \frac{1}{i} = \frac{1}{f},$$

or

$$i^2 - id + fd = 0.$$

The roots of this quadratic equation are

$$i = \frac{d \pm \sqrt{d^2 - 4fd}}{2}.$$

As the image is real, the roots have to be real and positive. This imposes the condition that

$$d^2 - 4fd \geq 0,$$

or

$$d \geq 4f.$$

