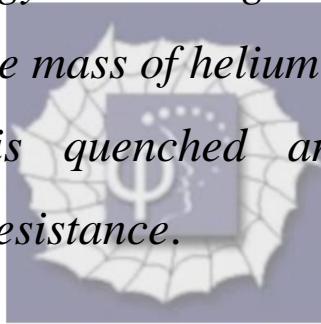


524.

Problem 38.35 (RHK)

The coil of a superconducting electromagnet used for nuclear magnetic resonance investigations has an inductance of 152 H and carries a current of 32 A. The coil is immersed in liquid helium, which has a latent heat of vaporization of 85 J per mole. (a) We have to calculate the energy in the magnetic field of the coil. (b) We have to find the mass of helium that is boiled off if the superconductor is quenched and thereby suddenly develops a finite resistance.



Solution:

The energy stored in the magnetic field in an inductor of inductance L when a current i is flowing through it is

$$U = \frac{1}{2} Li^2.$$

In our problem

$$L = 152 \text{ H,}$$

and

$$i = 32 \text{ A.}$$

Therefore, the energy stored in the magnetic field

$$U = \frac{1}{2} \times 152 \times 32^2 \text{ J} = 778 \text{ kJ.}$$

The latent heat of vaporization of helium is 85 J per mole.

The amount of helium vaporized by 778 kJ of energy will be

$$m = \frac{77.8 \times 10^3}{85} \text{ mole} = 915.6 \text{ mole.}$$

Mass of 1 mole of helium is 4 g. Therefore, the mass of 915.6 mole of helium will be $M = 915.6 \times 4 \text{ g} = 3.66 \text{ kg}$.

This amount of helium will be boiled off by the energy stored in the inductor when the superconductor is quenched.