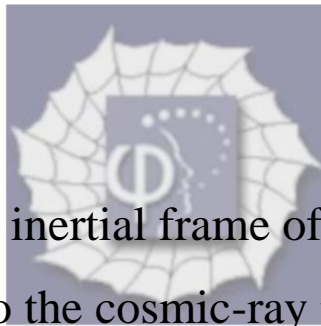


182.

Problem 2.33 (R)

One cosmic-ray particle approaches the Earth along its axis with a velocity of $0.8 c$ toward the North Pole and another with a velocity $0.6 c$ toward the South Pole. We have to find the relative speed of approach of one particle with respect to the other.

Solution:



Let us consider an inertial frame of reference which is at rest with respect to the cosmic-ray particle which to an observer on Earth is approaching it along its axis toward the North Pole. Let us call this frame of reference S . with respect to this frame of reference the inertial frame of reference in which the Earth is stationary, S' , will be moving toward it with velocity $v = 0.8 c$. In S' another cosmic ray particle is observed moving in the direction of the south-north axis with velocity $u = 0.6 c$.

We have to calculate the speed of the other cosmic-ray particle, u' , as measured by an observer in S . This speed will be the relative speed between the two cosmic-ray particles.

According to the velocity addition theorem

$$u' = \frac{u + v}{1 + uv/c^2} = \frac{0.6 + 0.8}{1 + 0.6 \times 0.8} c = 0.946 c.$$

