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Problem 21.1 (RHK)

Quite apart from effects due to the Earth's rotational and orbital motions, a laboratory frame is not strictly an inertial frame because a particle placed at rest there will not, in general remain at rest; it will fall under gravity. Often, however, events happen so quickly that we can ignore free fall and treat the frame as inertial. Consider, for example, a 1.0-MeV electron (for which $v = 0.941 c$) projected horizontally into a laboratory test chamber and moving through a distance of 20 cm. We have to find (a) the time it would take to travel 20 cm and (b) the distance the electron would fall during this interval. We have to comment on the suitability of the laboratory as an inertial frame in this case.

Solution:

(a)

The speed of 1.0-MeV electron is $0.941 c$. The electron has been projected horizontally into a laboratory test

chamber and it moves through a distance of 20 cm Time taken by the electron to travel 20 cm will be

$$t = \frac{0.2}{0.941 \times 3 \times 10^8} \text{ s} = 7.1 \times 10^{-10} \text{ s}.$$

(b)

In this time the electron would have dropped vertically because of the surface gravity of the Earth by distance

$$y = \frac{1}{2} g t^2 = \frac{1}{2} \times 9.81 \times (7.1 \times 10^{-10})^2 \text{ m} = 2.5 \times 10^{-18} \text{ m}.$$

(c)

We can therefore safely conclude that effects of the Earth's gravity will be insignificant and as time intervals involved in relativistic motion of elementary particles are of the order of 10^{-10} s, non-inertial effects due to Earth's rotational and orbital motions will also be negligible and thus the laboratory can be treated as an inertial frame.