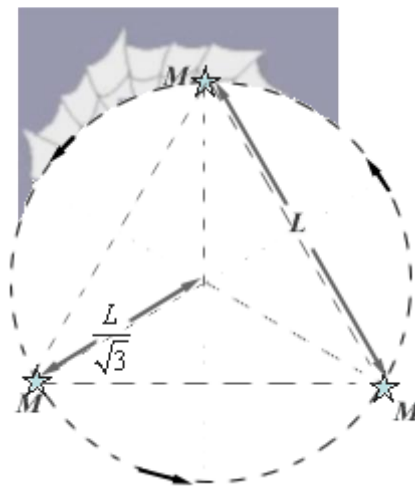


98.

**Problem 16.73 (RHK)**

*Three identical stars of mass  $M$  are located at the vertices of an equilateral triangle with side  $L$ . We have to find the speed with which they all revolve under the influence of one another's gravity in circular orbit circumscribing, while still preserving, the equilateral triangle.*



**Solution:**

It is a three-body problem, which lends itself to a solution. Three stars each of mass  $M$  revolve under the influence of one another's gravitational field in circular orbit. Let  $v$  be the speed of each star while revolving in a circular orbit of radius  $L/\sqrt{3}$ . The required centripetal

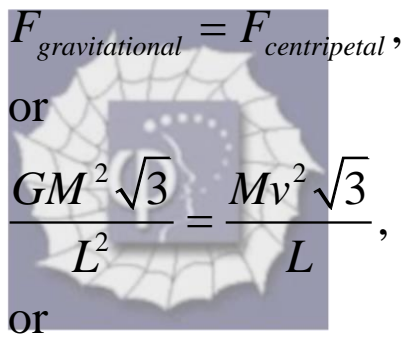
force for circular motion is

$$F_{\text{centripetal}} = \frac{Mv^2}{L/\sqrt{3}}.$$

The centripetal force on each star is provided by the resultant gravitational force due to the other two stars, which is

$$F_{\text{gravitational}} = 2 \times \frac{GM^2}{L^2} \cos \frac{\pi}{6} = \frac{GM^2 \sqrt{3}}{L^2}.$$

Equation of motion of each star is


$$F_{\text{gravitational}} = F_{\text{centripetal}},$$

or

$$\frac{GM^2 \sqrt{3}}{L^2} = \frac{Mv^2 \sqrt{3}}{L},$$

or

$$v = \sqrt{\frac{GM}{L}}.$$