43. 

## Problem 13.20P (HRW)

Two identical, uniform, frictionless spheres, each of weight $W$, rest in a rigid rectangular container. We have to find in terms of $W$, the forces acting on the spheres due to (a) the container surfaces and (b) one another, if the line of centres of the spheres makes an angle of $45^{\circ}$ with the horizontal.


## Solution:



We will first draw the free-body diagram of the ball 1. In this diagram $F$ is the force on the ball exerted by the wall, and $T$ is the force exerted by the ball 2 on the ball 1 . As the spheres are frictionless, force $T$ will be along their line of contact, which is at an angle of $45^{\circ}$ with the horizontal.

As the ball is in equilibrium, the vector sum of forces has to be zero. Adding the vertical component of forces, we get
$T \cos 45^{\circ}=W$,
or,
$T=\sqrt{2} W$.
Adding the horizontal component of forces acting on ball
1 , we get
$F=T \cos 45^{\circ}=T / \sqrt{2}=W$.
We will consider next the free-body diagram of ball 2 . It is as shown on the line diagram.

$N$ is the force exerted by the base of the box on the ball 2. $F$ is the force exerted by the side on the ball and $T$ is the force
exerted by the ball 1 on ball 2. Applying the conditions of static equilibrium, we get the following two equations:
$N=W+\frac{1}{\sqrt{2}} T=W+W=2 W$,
and
$F=\frac{1}{\sqrt{2}} T=W$.

